







FRANK J. SEILER RESEARCH LABORATORY

TECHNICAL REPORT FJSRL-TR-80-0019

DECEMBER 1980

THEORETICAL MODELING OF SCOT COLUMNS

Robert H. Fogelsong



APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED.

PROJECT 2303

AIR FORCE SYSTEMS COMMAND
UNITED STATES AIR FORCE

FJSRL-TR-80-0019

This document was prepared by the Energetic Materials Division, Directorate of Chemical Sciences, Frank J. Seiler Research Laboratory, United States Air Force Adademy, CO. The research was conducted under Project Work Unit Number 2303-F3-01, Maj Robert H. Foglesong was the Project Officer in charge of the work.

When U.S. Government drawings, specifications or other date are used for any purpose other than a definitely related government procurement operation, the government thereby incurs no responsibility nor any obligation whatsoever, and the fact that the government may have formulated, furnished or in any way supplied the said drawings, specifications or other data is not so be regarded by implication or otherwise, as in any manner licensing the holder or any other person or corporation or conveying any rights or permission to manufacture, use or sell any patented invention that may in any way be related thereto.

Inquiries concerning the technical content of this document should be addressed to the Frank J. Seiler Research Laboratory (AFSC) FJSRL/NC, USAF Academy, CO. 80840. Phone AC 303,472-2655.

This report has been reviewed by the Commander and is releasable to the National Technical Information Service (NTIS). At NTIS it will be available to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.

ROBERT H. FOGLESONG, Maj, USAF

Project Officer

KENNETH E. SIEGENTHAM

Director

Directorate of Chemical Sciences

Lt Col, USAF

Commander

Copies of this report should not be returned unless return is required by security considerations, contractual obligations, or notice on a specific document.

Printed in the United States of America. Qualified requestors may obtain additional copies from the Defense Documentation Center. All others should apply to: National Technical Information Service 5285 Port Royal Road

Springfield, Virginia 22161

UNCLASSIFIED SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)	SKI-TR-84-6019
REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
	3. RECIPIENT'S CATALOG NUMBER
FJSRL-TR-0019 ADA094707	5. TYPE OF REPORT & PERIOD COVERED
	FINAL rept
Theoretical Modeling of SCOT Columns.	1 Jul 57 — 30 Sep 80
	B. PERFORMING DAG. REPOST NOMBER
7. 48THOR(3)	8. CONTRACT OR GRANT NUMBER(S)
	(17/E>/
Maj Robert H. Foglesong	10. PROGRAM ELEMENT, PROJECT, TASK
Frank J. Seiler Research Laboratory	AREA & WORK UNIT NUMBERS
U.S. Air Force Academy, Colorado 80840	23Ø3-F3-01
11 CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE
Frank J. Seiler Research Laboratory	November 1980
U.S. Air Force Academy, Colorado 80840	13. NUMBER OF PAGES
14 MONITORING AGENCY NAME & ADDRESS(II different from Controlling Office)	15. SECURITY CLASS. (of this report)
1(11) 1) 62 84 / 111	WW. 1.00.
	UNCLASSIFIED 15a. DECLASSIFICATION DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report)	
UNLIMITED	
	1
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from	Penert
77. DISTRIBUTION STATEMENT (OF the abstract entered in block 20, it different from	(Кероп)
	}
18. SUPPLEMENTARY NOTES	
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)	
Chromotographic Theory	
Heats of Vaporization Boiling Points	
Support Coated Open Tubular (SCOT) Chromatography	
Thermodynamics	
A description of the thermodynamic processes that oc	cur within a SCOT column is
presented. The unique geometry of the SCOT column w	as found to slightly alter
the mathematical description of the thermodynamic ph	
traditional packed column. The correlation derived description was used to determine experimental value	
tion and boiling points for several light alcohols t	
and validity.	* * * * * * * * * * * * * * * * * * *
DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE	714920

3 19120 + SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

SECURITY CLASSIFICATION OF THIS PAGE(When Data Entered)	
ļ	
1	
: !	
	į
	1
	{
	,
	Į.
	ì

SUMMARY

The use of thermodynamics and physical chemistry as applicable to SCOT column phenomenon is applied as a modeling technique to derive a correlation suitable for calculation of heats of vaporization and boiling points for SCOT column geometry. Beginning with the expression for partial pressure as given in terms of activity coefficients, mole fraction in a solution and vapor pressure of the solute, and then applying various algebraic substitutions, correlating several chromatographic expressions and incorporating SCOT column peculiarities, an expression has been derived that permits the easy calculation of heats of vaporization and boiling points. The mathematical derivation closely parallels the theory associated with packed chromatographic columns, yet incorporates discussions and physical application of factors particular to SCOT columns to modify/confirm the usefulness of packed column theory for SCOT column applications. Experimental work as derived from a SCOT column in a Perkin-Elmer chromatograph is supplied to permit utilization of said correlation and to verify its validity.

Accession For	
NTIS GRAAL	
TIC TE	[_]
រីកសាធនយាមនាធិ	; ,
Jactification	L
Distribution	7 Octos
$E_{i}(z,\lambda,\zeta,t)$	
Ave. No. 1	
Ave. Sec. 1	

TABLE OF CONTENTS

SECTION	PAGE
SUMMARY	1
TABLE OF CONTENTS	2
INTRODUCTION	3
THERMODYNAMIC DERIVATION	4-6
RESULTS	7
CONCLUSIONS	8
REFERENCES	9
NOMENCLATURE	10-11

INTRODUCTION

The use of column chromatography as as analytical tool has increased at a significant rate and has resulted in many practical applications throughout industry. Many examples of appropriate applications include the use of gas-liquid chromatography for the determination of transport and/or thermodynamic properties, the use of chromatography for the purification of small commercial quantities of speciality chemicals, and the use of gas chromatography as the primary analytical device for direct measurement and control of continuous processes.

Thus, the ever-increasing need for better column performance has brought about the introduction of a new concept in gas-liquid chromatographic columns. The support coated open tubular column (SCOT) has presented researchers and practical applications experts with a tool that combines the advantages of the traditional packed column and those of the open tubular design. Advantages gained through reductions in analysis times and significantly smaller pressure drops have increased the popularity of the SCOT column. Better separation capabilities and larger sample sizes associated with the SCOT column have permitted many practical applications not previously possible.

As was characteristic of a young idea in science, the theoretical study and analysis of this analytical tool lagged practical applications of the SCOT column. Numerous papers are available directly related to practical applications of SCOT geometry. Theoretical studies are limited but becoming more available. The SCOT column itself has been partially responsible for this limited amount of published theory. The complex mathematical description of the support layer adhering to the column wall has not lent itself to easy solution. Thus, one of the goals of this work will be to apply some basic thermodynamic principles as applicable to packed column geometry and to modify the results in order to obtain a suitable description of parallel thermodynamic occurrences within SCOT columns. This particular application will result in the use of said thermodynamic theory to derive the physical properties (Tb and \triangle Hv) of several simple alcohols as a verification of the applicability of the theory ulitized to describe intercolumn phenomenon.

To achieve different results, numerous researchers have applied the use of modeling and thermodynamic theory with packed columns. As examples, the use of gas-liquid chromatography was used by Hoare and Purnell (1,2) to evaluate vapor pressure, boiling points, latent heats and entropies of solution. Their work closely parallels the thermodynamic applications to be presented in this article. Littlewood, et al. (3) measured heats of solution from chromatographic data. The calculation of dispersion coefficients by means of moments has been done by Horn (4), while Giddings, et al. (5) determined values for gaseous diffusion coefficients by using theoretical correlations based on chromatographic theory.

THERMODYNAMIC DERIVATION

As has been commonly done in past thermodynamic modeling of packed column geometry, it will be assumed that the partial pressure of the solute over the solution within a SCOT column can be described by the following equation:

$$p = p^{\circ} \chi x \tag{1}$$

where p is the partial pressure of the solute over the solution, χ is the activity coefficient, x is the mole fraction in solution and p is the vapor pressure of the solute. The partial pressure of the solute over the solution can also be expressed as follows:

$$p = C_g^s R T (2)$$

where C_g^s is the molar concentration of the solute in the gas phase. The mole fraction in the solution can be represented by the following equation:

$$x = N_1^s / N_1 + N_1^s \approx N_1^s / N_1$$
 (3)

where N_1^s is the number of moles of solute in solution in N_1 moles of solvent. Since N_1 is equal to the volume of solvent (V_1) divided by the molar volume (V_1) , the following expression can be algebraically derived from equation (3):

$$x = N_1^s V_1^m / V_1 = C_1^s V_1^m$$
 (4)

Substituting equations (2) and (4) into equation (1) yields the following:

$$C_1^s / C_g^s = K = R T / V_1^m \gamma p^o$$
 (5)

where K is the familiar partition coefficient. Then, by definition,

$$v_{R} = K v_{1}$$
 (6)

where V_R is the net retention volume. Therefore,

$$V_{R} = (R T / V_{p}^{o})(V_{1} / V_{1}^{m}) = (R T / V_{p}^{o})(w / M_{1})$$
 (7)

where w is the grams of solute and M_1 is the molecular weight of the solute. Therefore the retention volume/gram weight of solute is

$$v_{p}^{T} = R T / \mathcal{Y}_{p}^{O} M_{1}$$
 (8)

The specific retention volume is also defined by Ambrose, et al. (6) as

$$v_g = 273 v_R^T / T$$
 (9)

Therefore,

$$v_g = (273 \text{ R}) / (\chi_p^0 M_1)$$
 (10)

or

$$V_g = 1.7 \times 10^7 / \chi_{p^0} M_1$$
 (11)

where $X = X_a$ X_t . As another thermodynamic principle is applied, at equilibrium,

$$dG_{\text{vap}} = dG_{\text{liq}} \tag{12}$$

where G is Gibbs free energy, and

$$dG = v dp - s dT (13)$$

where v is the volume per mole of pure substance and s is the entropy per mole of pure substance. Therefore, from equations (12) and (13),

$$dp / dT = (S_1 - S_y)/(V_1 - V_y)$$
 (14)

but,

$$\Delta S = \Delta_{H_{V}} / T \tag{16}$$

where Δ_{ll} is the heat of vaporization of the solute. Therefore,

$$dp / dT (V_1 - V_v) = \Delta H_v / T$$
 (16)

From general chromatographic theory the following correlation can be derived:

$$V_1 - V_v = V_1 (1 - \beta) = (RT/p)(1/\beta - 1)$$
 (17)

where β is the total volume of gas in a **c**olumn divided by the total volume of liquid in a column. This correlation will thus allow for the unique geometry of the SCOT column as will later be discussed. Therefore,

$$dp / dT (R T / p)(1 / \beta - 1) = \Delta_{H_v} / T$$
 (18)

or

$$d \ln p / dT = (\Delta H_v / R T^2) (\beta / 1 - \beta)$$
 (19)

if $\Delta H_{v} \neq f(T)$,

$$p^{\circ} = \exp(\Delta H_{V} / R T (\beta / \beta - 1) + 2.3 C)$$
 (20)

Referring back to equation (11), it now becomes necessary to develop an expression for χ_T . Khan (7) has verified the following expression for χ_T :

$$\ln \chi_{T} = \Delta H_{M} / R T \qquad (21)$$

where ΔH_{M} is the heat of mixing. Therefore, combining equations (20) and (21) results in the following relationship:

where

$$a = (\Delta H_M + \Delta H_v(\beta/\beta - 1)) / \Delta H_v$$

a = constant for an ideal solution

Substitution of equation (22) into equation (11) yields the following:

$$v_{g} = \frac{1.7 \times 10^{7}}{\chi_{a} M_{1} (p^{0})^{a} \exp (2.3 C (1 - a))}$$
 (23)

or

$$log V_g = -A log p^o + C$$

Therefore, by using previous definitions for p^{o} ,

$$\log V_g = A' (\Delta H_v / R T)(\beta / \beta - 1) + D \qquad (24)$$

An expression similar to equation (24) has been derived for packed columns (1,2) and used to calculate \triangle H with reasonable success. The above relationship was derived by using the same thermodynamic relationships as has been applied by previous researchers. The inclusion of the β term as it applies to SCOT column geometry modified a portion of the packed column derivation. This modification was significant and proved to provide an additional term as the derivation proceeded. The final result would thus indicate SCOT columns can be used in exactly the same way as packed columns to obtain experimental values of \triangle H and T (boiling point) via the following expression:

$$\Delta H_v / T_b = constant (Trouton)$$
 (25)

RESULTS

The experimental results necessary to verify the usefulness of equation (24) was obtained from a Perkin-Elmer Model 990 Gas Chromatograph. The actual separation device was a fifty foot, .020 inch diameter SCOT column containing a Carbowax 1540 liquid phase. A β factor of fifty was used to characterize this column. Various physical modifications were incorporated to allow those measurements necessary to supply data permitting the calculation of the partition coefficient (K). Ethanol and isopropyl alcohol were used as liquid samples. Temperature was varied, permitting the determination of K , and consequently V , over a fairly significant temperature range. A plot of log V $_{\rm S}^{\rm G}$ versus 1/T was constructed. The resulting slope must be equal to the following expression:

Slope =
$$(\beta / \beta - 1)(\Delta H_v / R)$$

The results of the mathematical determination of both $\Delta_{\rm H}$ and T are presented in Table 1. Comparative values of both parameters are presented as obtained from Perry's Chemical Engineer's Handbook (8).

 $\begin{array}{cccc} \underline{\mathtt{TABLE} & 1} \\ \\ \mathtt{COMPARATIVE} & \mathtt{VALUES} & \mathtt{OF} & \mathtt{H} & \mathtt{AND} & \mathtt{T}_{\mathtt{b}} \end{array}$

Parameter	<u>Ethanol</u>	Isopropyl Alcohol
T _b (this work-K ^o)	345	356
T _b (Perry's-K ^o)	351	365
$\Delta_{ ext{W}}^{ ext{H}}$ (this work-cal/m)	9240	9520
△H _v (Perry's-cal/m)	9304	9550

CONCLUSIONS

The applicability of many of the same thermodynamic relationships for packed chromatographic columns to SCOT column geometry is apparent. By thermodynamically modeling a SCOT column in much the same manner as has been accomplished for packed columns and incorporating an appropriate modification to account for the extreme ratio of $V_{\rm g}/V_{\rm l}$ in a SCOT column as opposed to a packed column, it was determined that the incorporation of said modification would slightly modify the final thermodynamic relationship. This final relationship was similar to that obtained for a packed column. The usefulness and validity of the SCOT column geometry associated relationship has been demonstrated by the fairly accurate results obtained by combining said relationship with experimental results obtained from the labratory.

REFERENCES

- Hoare, M. R., and Purnell, J. H., Research, 8 p. 841 (1955).
- 2. Hoare, M. R., and Purnell, J. H., Transactions of the Faraday Society, <u>52</u> p. 272 (1956).
- 3. Littlewood, A. B., Phillips, C. S. G., and Price, D. T., Journal of the Chemical Society, p. 1480 (1955).
- 4. Horn, F. J. M., "Calculation of Dispersion Coefficients by Means of Moments", paper submitted to AIChE Journal, presented at the 58th National AIChE Metting, Dallas, Texas, (1966).
- 5. Giddings, J. C., and Seager, S. L., Industrial and Engineering Chemistry Fundamentals, $\frac{1}{2}$ p. 277 (1962).
- 6. Ambrose, R. , Keulmans, A. I. M. and Purnell, J. H., Analytical Chemistry, 30 p. 1582 (1958).
- 7. Khan, M. A., Gas Chromatography, Butterworths, London, ed. D. H. Desty, p. 135 (1958).
- 8. Perry, R. H., Chilton, C. H., and Kirkpatrick, S. D., Chemical Engineering Handbook, 4th Edition, p. 3-113 (1963).

NOMENCLATURE

- a $(\Delta H_M + \Delta H_V (\beta/\beta 1)/\Delta H_V$
- A Constant
- C Integration Constant
- CS Concentration of solute in gaseous phase
- C, Concentration of solute in solvent
- D Integration Constant
- G Gibbs Free Energy
- $\triangle H_{M}$ Heat of Mixing
- $\triangle \mathbf{H}_{_{\mathbf{tr}}}$ Heat of Vaporization
- K Partition Coefficient
- M Molecular Weight of Solvent
- N, Moles of Solvent
- N^S Moles of Solute in Solution
- p Partial Pressure
- o Vapor Pressure
- R Gas Constant per Mole
- s Entropy per Mole of Pure Substance
- △S Entropy of System
- T Temperature
- T Normal Boiling Point
- v Volume per Mole of Pure Substance
- V Specific Retention Volume
- V, Volume of the Liquid Phase
- v, Molar Volume

- $\mathbf{v}_{R}^{\mathbf{T}}$ Retention Volume/Gram Weight of Solvent
- V_R Net Retention Volume
- V_ Volume of Gaseous Phase
- w Grams of Solvent
- x Mole Fraction in Solution
- β Beta Factor
- Activity Coefficient
- Concentration Dependent Activity Coefficient
- Ym Temperature Dependent Activity Coefficient

